

1. Let $\boldsymbol{R}$ be the region in the first quadrant bounded by the $x$-axis and the graphs of $f(x)=x+3$ and $g(x)=-x^{2}+4$. Region $S$ is bounded by the two curves and region $\boldsymbol{M}$ is bounded by the two curves and the $x$-axis in the second quadrant.
a. Find the area of $\boldsymbol{R}$.
b. Find the area of $\boldsymbol{M}$.
c. Find the volume of a solid when area $\boldsymbol{S}$ is rotated about the line $y=5$.
d. Region $\boldsymbol{S}$ is the base of a solid. For the solid, each cross section perpendicular to the $x$-axis is an equilateral triangle. Write but do not solve an integral expression for the volume of this solid.
